



Dinamik Dengeleme Çalışmaları

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ODTÜ Makina Mühendisliği Bölümü, Ankara

Statik Dengeleme

Bir mekanizmada uzuvların ağırlığı ve esnekliği gibi etmenlerin dengelenerek mekanizmanın herhangi bir konumda statik dengede kalabilmesi için statik dengeleme yapılır.

STATİK DENGELEME = SABİT SİSTEM POTANSİYEL ENERJİSİ

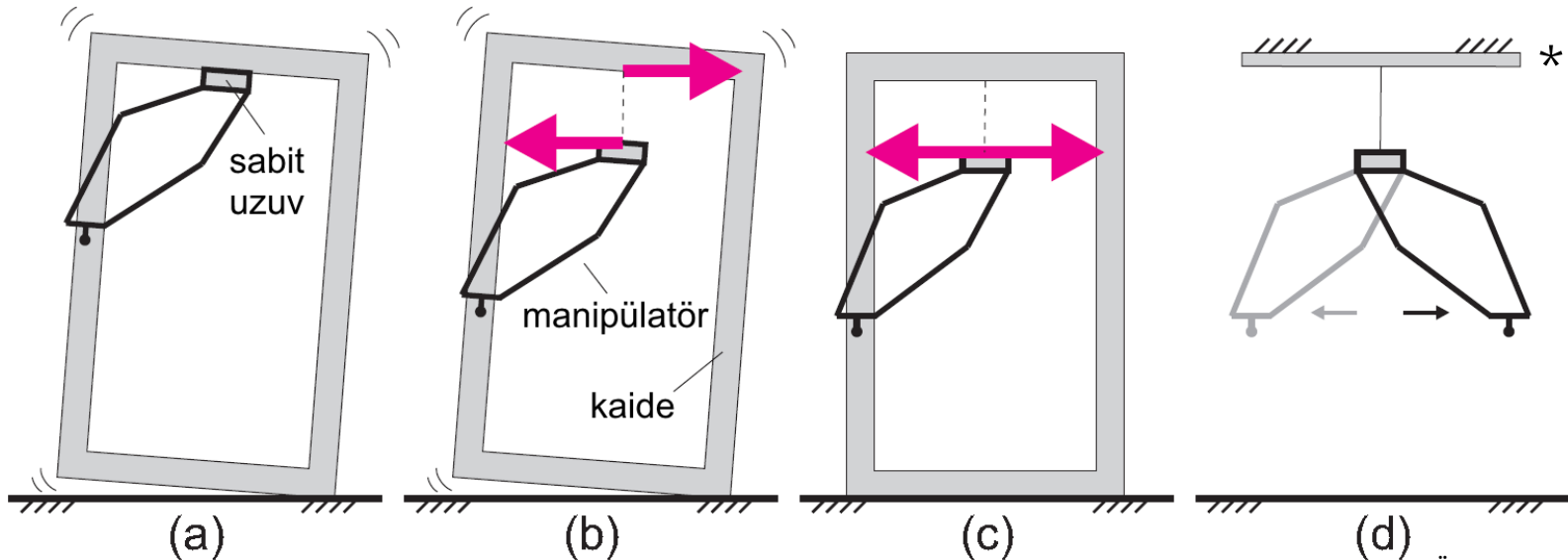


Statik dengelemede iki yaygın yöntem karşıt kütleler ile dengeleme ve yaylar ile dengelemedir.

Dinamik Dengeleme

Bir mekanizmada uzuvların atalet kuvvet/momentlerinden dolayı kaide oluşun sarsma kuvvet/momentlerini sıfırlamaya dinamik dengeleme denir.

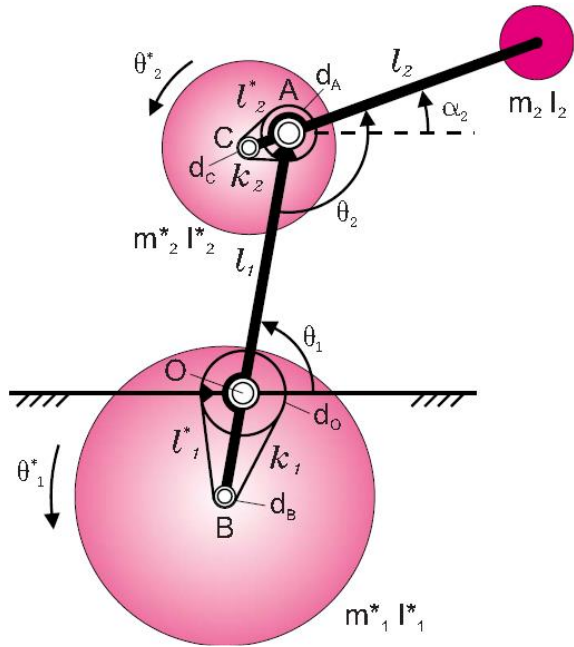
DİNAMİK DENGELEME = SABİT SİSTEM MOMENTUMU



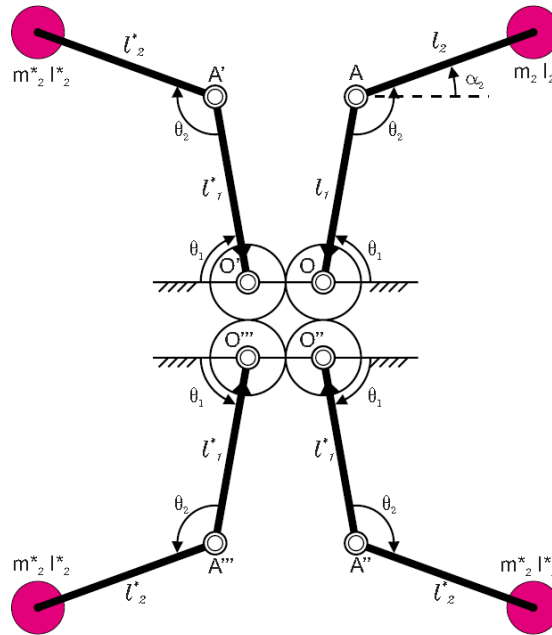
*Van der Wijk V (2014) Methodology for Analysis and Synthesis of Inherently Force and Moment-Balanced Mechanisms. Delft Üniversitesi Doktora Tezi

Dengelenmemiş manipülatör (a) kaidede sarsma kuvvet ve momentleri meydana getirir (b). Dinamik dengeleme ile sarsma etkileri sıfırlanabilirse manipülatör bir ipe bağlı olarak bile yüksek ivmelerde çok hassas çalışabilir.

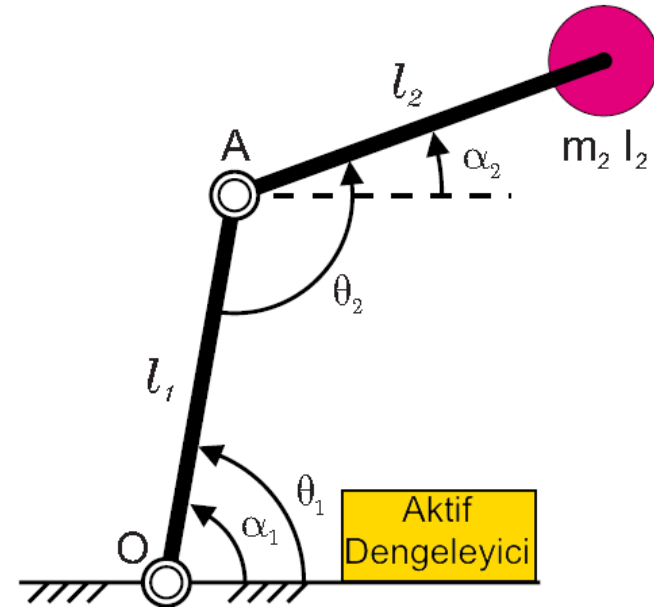
Dinamik Dengeleme Yöntemleri



Karşıt kütle/atalet momenti ile dengeleme

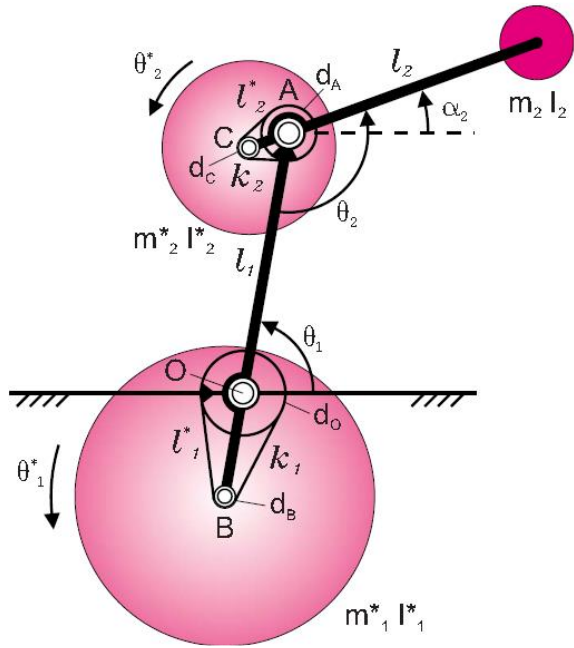


Mekanizma ayna görüntüsü ile dengeleme

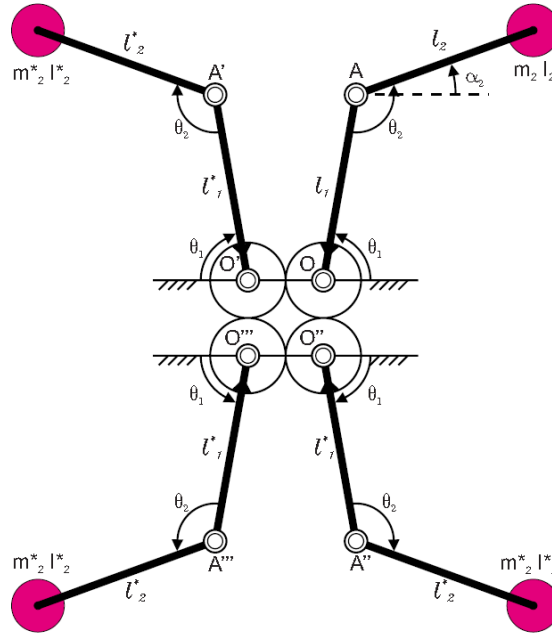


Aktif dengeleme

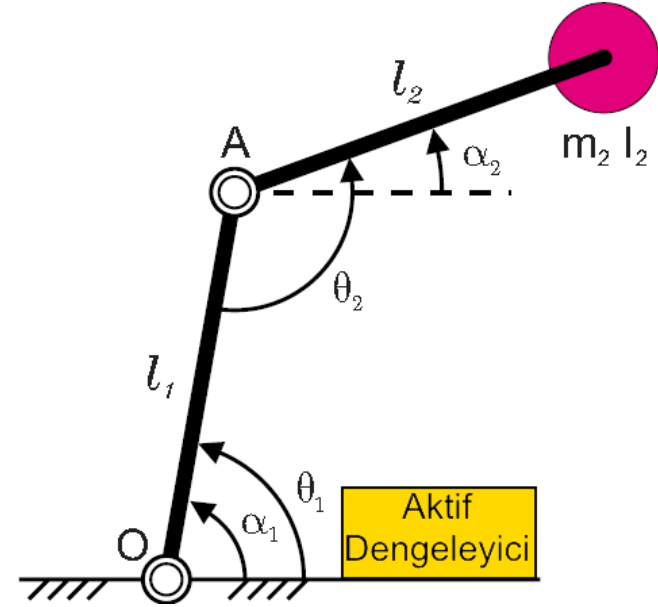
Dinamik Dengeleme Yöntemleri



Karşıt kütle/atalet momenti ile dengeleme

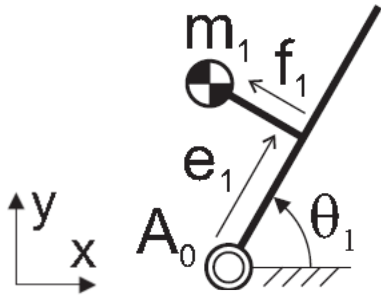


Mekanizma ayna görüntüsü ile dengeleme



Aktif dengeleme

Seri Zincirlerin Dengelenmesi



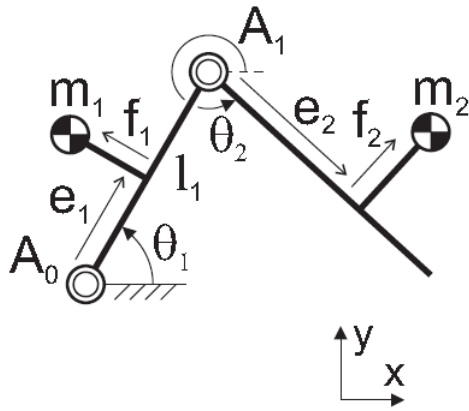
$$\bar{r}_1 = \begin{bmatrix} r_{1x} \\ r_{1y} \end{bmatrix} = \bar{A}_0 + \begin{bmatrix} e_1 \cos \theta_1 - f_1 \sin \theta_1 \\ e_1 \sin \theta_1 + f_1 \cos \theta_1 \end{bmatrix}$$

$$\text{Linear momentum: } \bar{L} = m_1 \dot{\bar{r}}_1 = \begin{bmatrix} -m_1 e_1 \sin \theta_1 - m_1 f_1 \cos \theta_1 \\ m_1 e_1 \cos \theta_1 - m_1 f_1 \sin \theta_1 \end{bmatrix} \dot{\theta}_1 = \begin{bmatrix} C_1 \\ C_2 \end{bmatrix}$$

Dinamik kuvvet dengesi koşulu: $m_1 e_1 = 0$ $m_1 f_1 = 0$

Ya uzuv baştan bu şekilde tasarlanır, ya da karşıt kütle ile dengeleme yapılır. Karşıt kütle dengelemesi sonrasında moment dengesi olumsuz etkilenir

Seri Zincirlerin Dengelenmesi



$$\bar{r}_1 = \begin{bmatrix} r_{1x} \\ r_{1y} \end{bmatrix} = \bar{A}_0 + \begin{bmatrix} e_1 \cos \theta_1 - f_1 \sin \theta_1 \\ e_1 \sin \theta_1 + f_1 \cos \theta_1 \end{bmatrix}$$

$$\bar{r}_2 = \begin{bmatrix} r_{2x} \\ r_{2y} \end{bmatrix} = \bar{A}_0 + \begin{bmatrix} l_1 \cos \theta_1 + e_2 \cos \theta_2 - f_2 \sin \theta_2 \\ l_1 \sin \theta_1 + e_2 \sin \theta_2 + f_2 \cos \theta_2 \end{bmatrix}$$

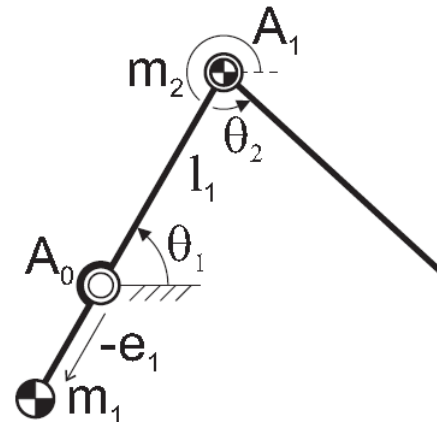
$$\bar{L} = m_1 \dot{\bar{r}}_1 + m_2 \dot{\bar{r}}_2 = \begin{bmatrix} -(m_1 e_1 + m_2 l_1) \sin \theta_1 - m_1 f_1 \cos \theta_1 \\ (m_1 e_1 + m_2 l_1) \cos \theta_1 - m_1 f_1 \sin \theta_1 \end{bmatrix} \dot{\theta}_1 + \begin{bmatrix} -m_2 e_2 \sin \theta_2 - m_2 f_2 \cos \theta_2 \\ m_2 e_2 \cos \theta_2 - m_2 f_2 \sin \theta_2 \end{bmatrix} \dot{\theta}_2 = \begin{bmatrix} C_1 \\ C_2 \end{bmatrix}$$

Lineer momentum:

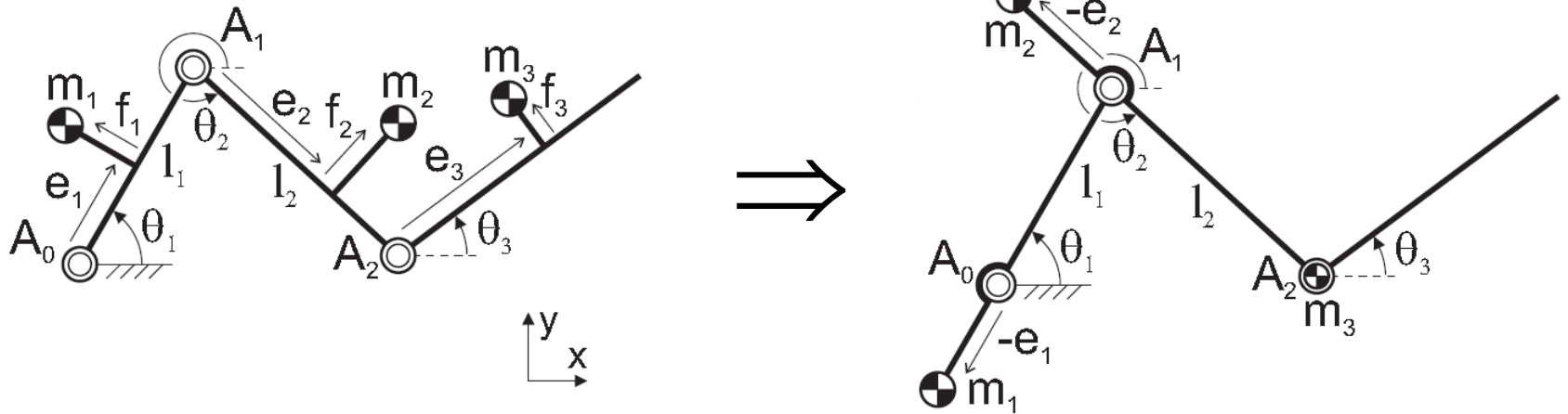
Dinamik kuvvet dengesi koşulları:

$$m_1 e_1 + m_2 l_1 = 0 \quad m_1 f_1 = 0$$

$$m_2 e_2 = 0 \quad m_2 f_2 = 0$$



Seri Zincirlerin Dengelenmesi



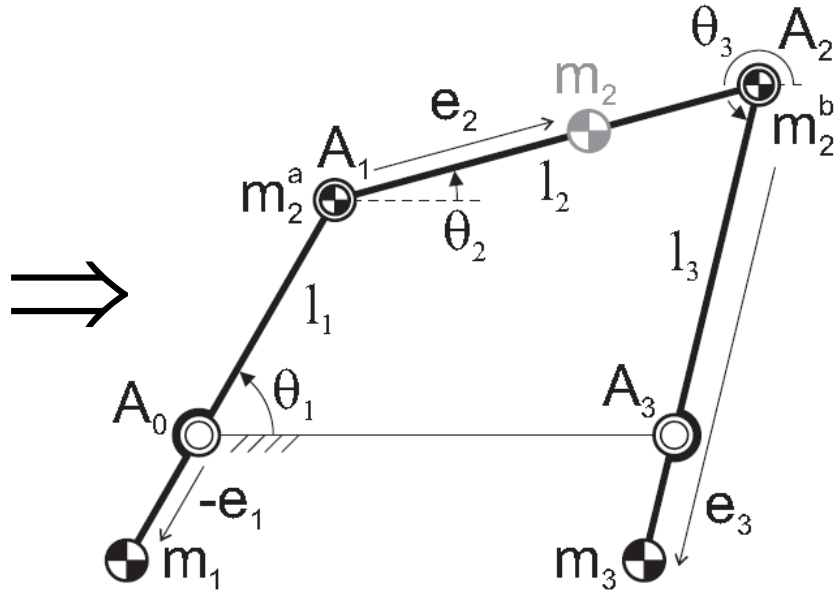
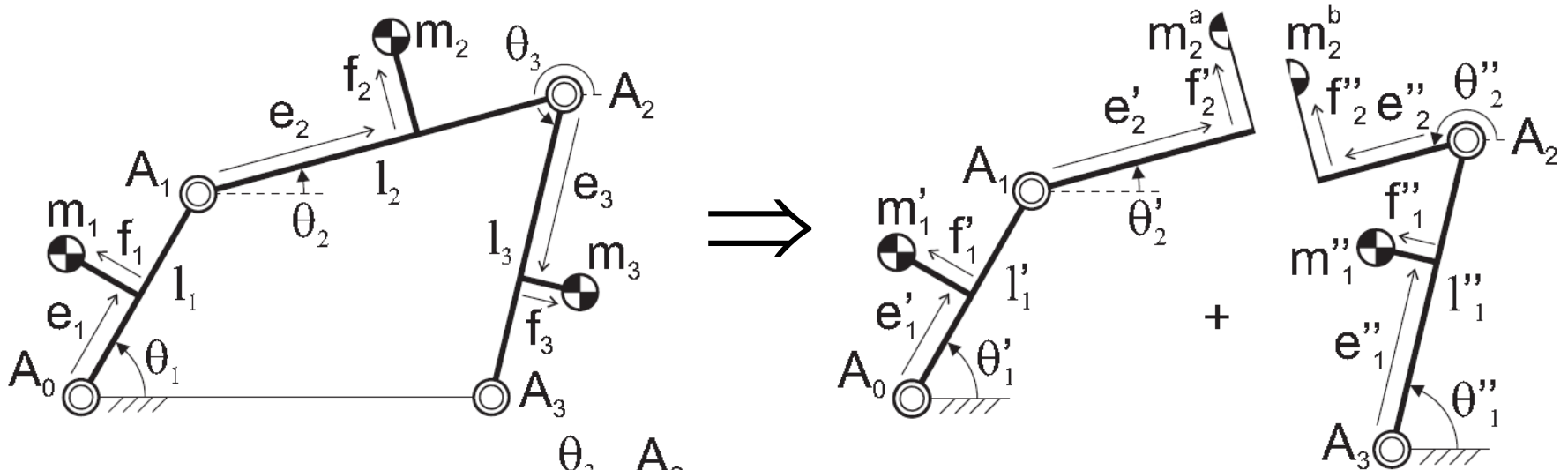
3 uzvunun kütle merkezi A_2 mafsalında (m_2), 2 ve 3 uzuvlarının toplam kütle merkezi A_1 mafsalında ($m_2 + m_3$), 1, 2 ve 3 uzuvlarının toplam kütle merkezi A_0 mafsalında ($m_1 + m_2 + m_3$) olmalı.

$$m_1 e_1 + m_2 l_1 + m_3 l_1 = 0 \quad m_1 f_1 = 0$$

$$m_2 e_2 + m_3 l_2 = 0 \quad m_2 f_2 = 0$$

$$m_3 e_3 = 0 \quad m_3 f_3 = 0$$

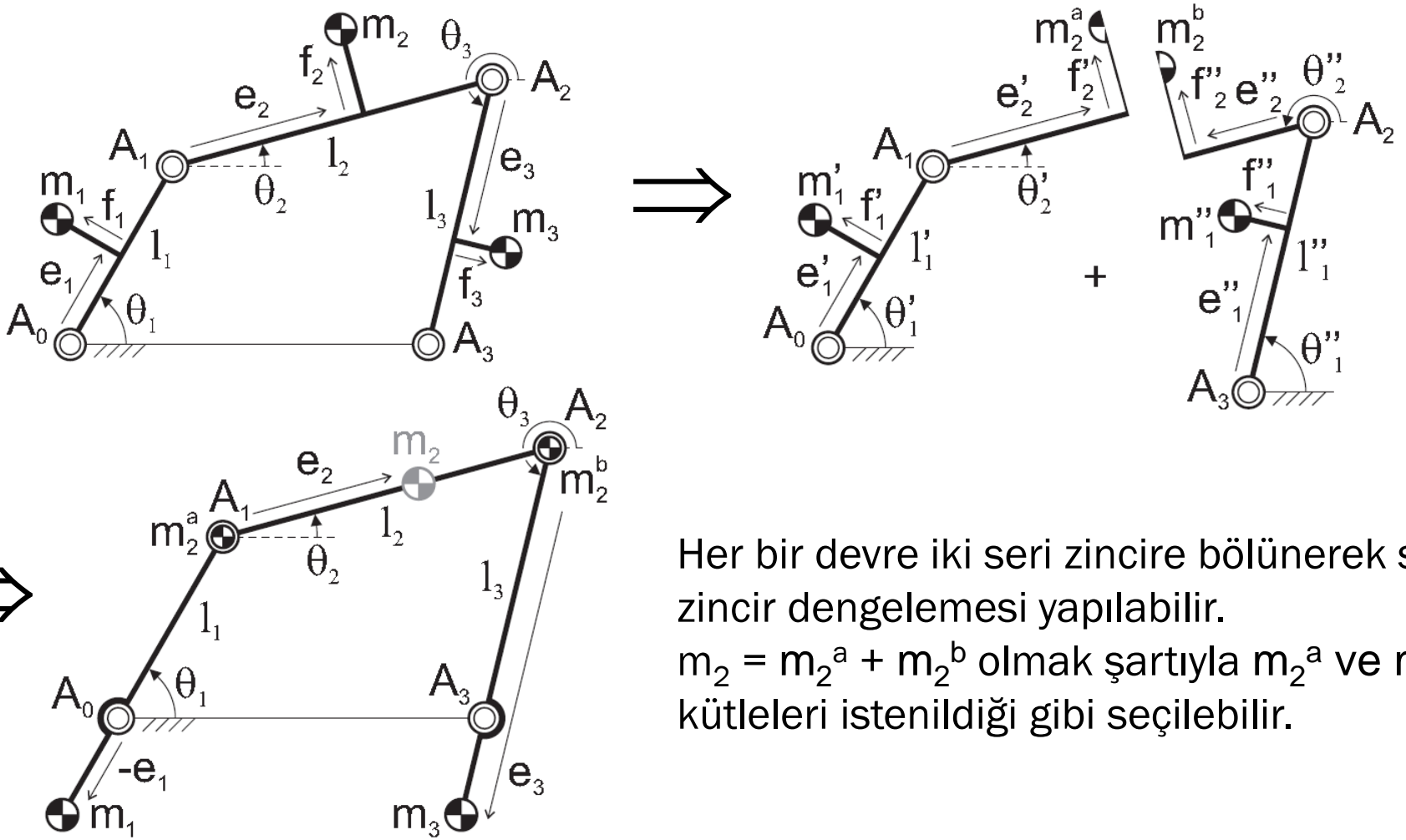
Kapalı Zincirlerin Dengelenmesi



Her bir devre iki seri zincire bölünerek seri zincir dengelemesi yapılabilir.
 $m_2 = m_2^a + m_2^b$ olmak şartıyla m_2^a ve m_2^b kütleleri istenildiği gibi seçilebilir.

Kapalı Zincirlerin Dengelenmesi

Yöntem 1: seri zincirlere bölme

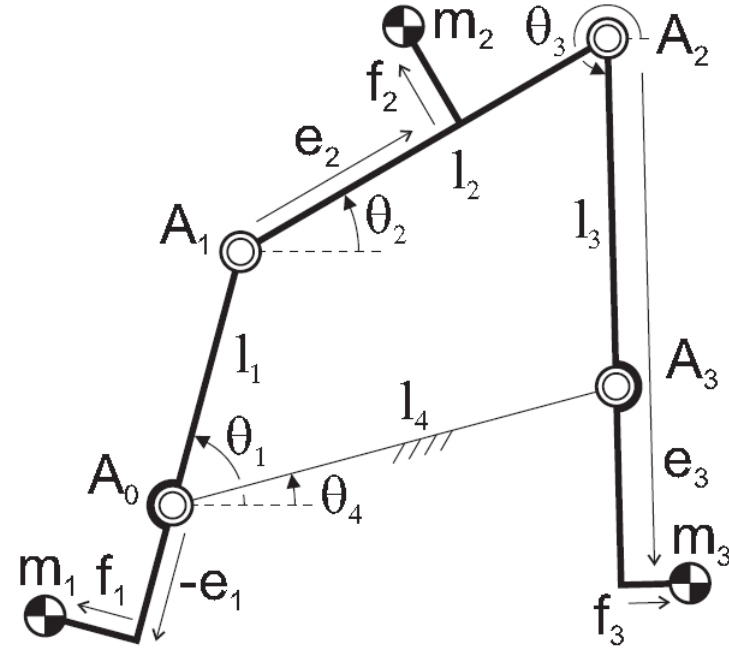
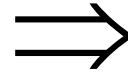
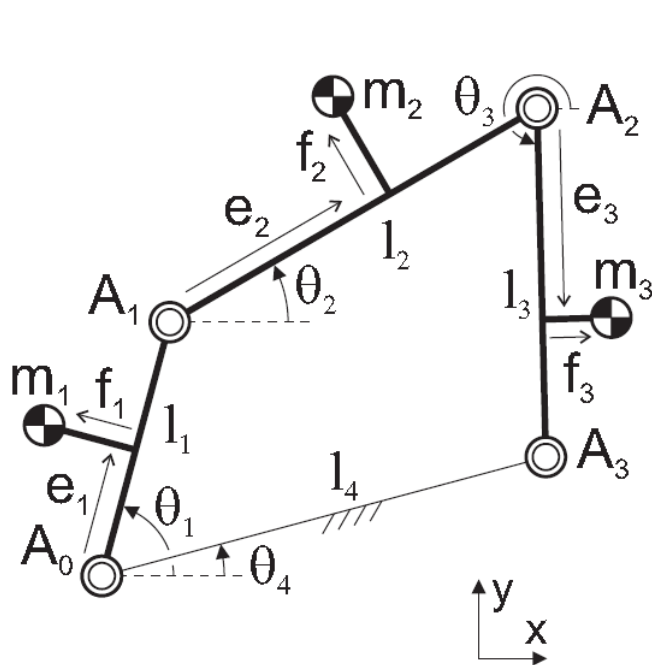


Her bir devre iki seri zincire bölünerek seri zincir dengelemesi yapılabilir.

$m_2 = m_2^a + m_2^b$ olmak şartıyla m_2^a ve m_2^b kütleleri istenildiği gibi seçilebilir.

Kapalı Zincirlerin Dengelenmesi

Yöntem 2: devre kapalılık denklemleri



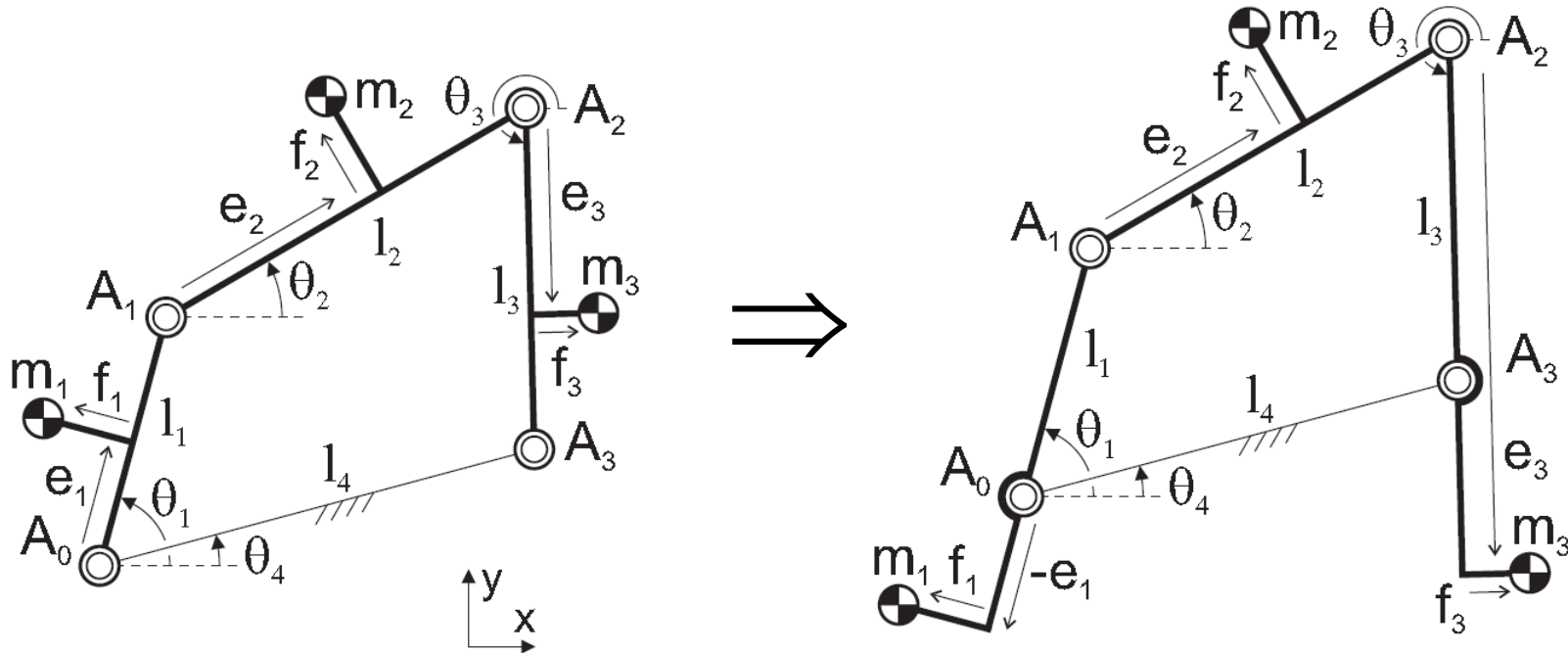
$$\bar{L} = \begin{bmatrix} -(m_1 e_1 + m_2 l_1 + m_3 l_1) \sin \theta_1 - m_1 f_1 \cos \theta_1 \\ (m_1 e_1 + m_2 l_1 + m_3 l_1) \cos \theta_1 - m_1 f_1 \sin \theta_1 \end{bmatrix} \dot{\theta}_1 + \begin{bmatrix} -(m_2 e_2 + m_3 l_2) \sin \theta_2 - m_2 f_2 \cos \theta_2 \\ (m_2 e_2 + m_3 l_2) \cos \theta_2 - m_2 f_2 \sin \theta_2 \end{bmatrix} \dot{\theta}_2 + \begin{bmatrix} -m_3 e_3 \sin \theta_3 - m_3 f_3 \cos \theta_3 \\ m_3 e_3 \cos \theta_3 - m_3 f_3 \sin \theta_3 \end{bmatrix} \dot{\theta}_3$$

Devre kapalılık denklemleri ve türevi:

$$\begin{aligned} l_1 \cos \theta_1 + l_2 \cos \theta_2 + l_3 \cos \theta_3 - l_4 \cos \theta_4 &= 0 \\ l_1 \sin \theta_1 + l_2 \sin \theta_2 + l_3 \sin \theta_3 - l_4 \sin \theta_4 &= 0 \\ \sin \theta_2 \dot{\theta}_2 &= -\frac{l_1}{l_2} \sin \theta_1 \dot{\theta}_1 - \frac{l_3}{l_2} \sin \theta_3 \dot{\theta}_3 \\ \cos \theta_2 \dot{\theta}_2 &= -\frac{l_1}{l_2} \cos \theta_1 \dot{\theta}_1 - \frac{l_3}{l_2} \cos \theta_3 \dot{\theta}_3 \end{aligned}$$

Kapalı Zincirlerin Dengelenmesi

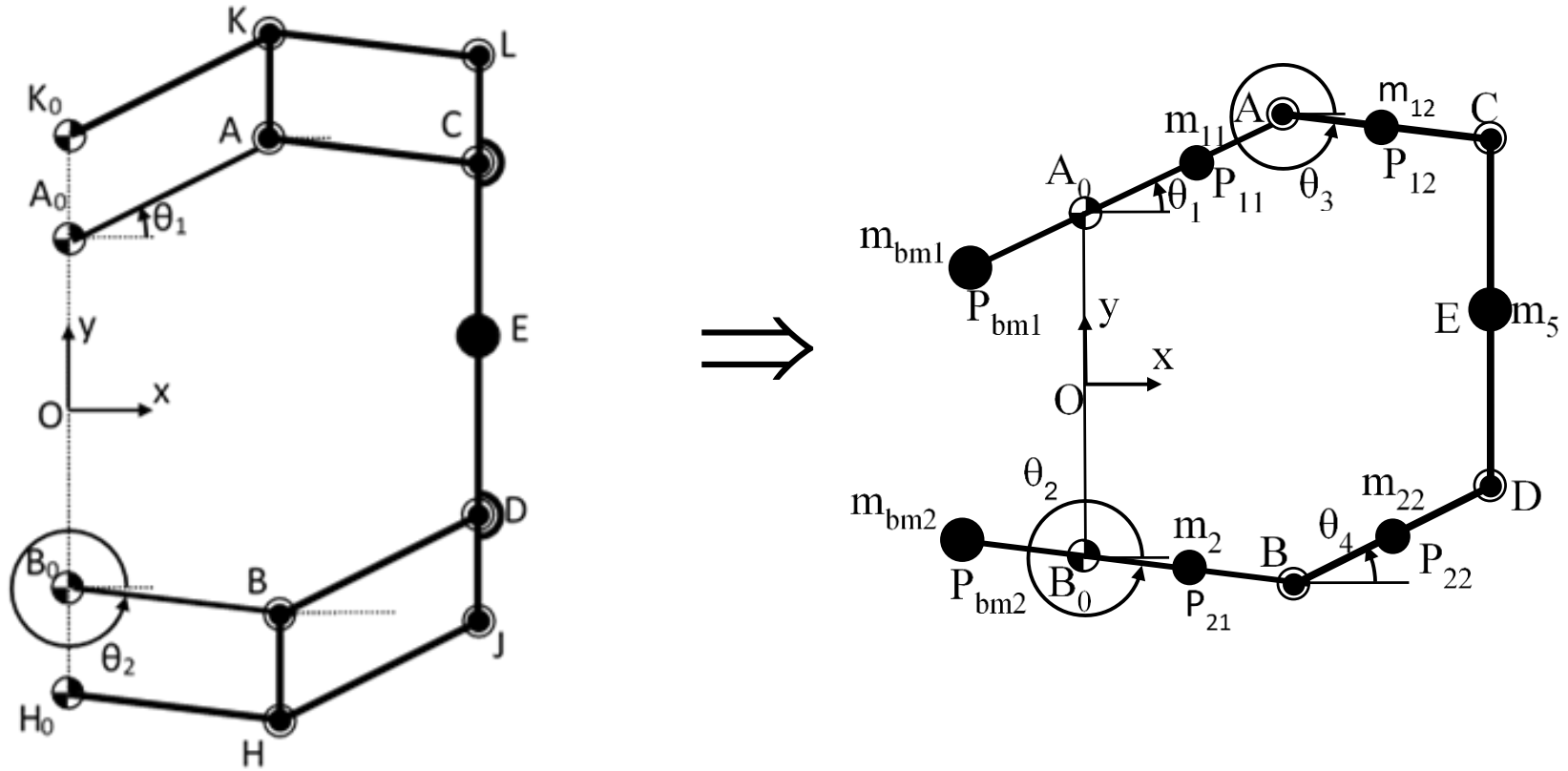
Yöntem 2: devre kapalılık denklemi



$$\bar{L} = \begin{bmatrix} -(m_1 e_1 + m_2 (1 - \frac{e_2}{l_2}) l_1) \sin \theta_1 - (m_1 f_1 - m_2 \frac{f_2}{l_2} l_1) \cos \theta_1 \\ (m_1 e_1 + m_2 (1 - \frac{e_2}{l_2}) l_1) \cos \theta_1 - (m_1 f_1 - m_2 \frac{f_2}{l_2} l_1) \sin \theta_1 \\ (m_3 (l_3 - e_3) + m_2 \frac{e_2}{l_2} l_3) \sin \theta_3 - (m_3 f_3 - m_2 \frac{f_2}{l_2} l_3) \cos \theta_3 \\ -(m_3 (l_3 - e_3) + m_2 \frac{e_2}{l_2} l_3) \cos \theta_3 - (m_3 f_3 - m_2 \frac{f_2}{l_2} l_3) \sin \theta_3 \end{bmatrix} \begin{matrix} \dot{\theta}_1 + \\ \dot{\theta}_3 \end{matrix} \text{Dinamik kuvvet dengesi koşulları:}$$

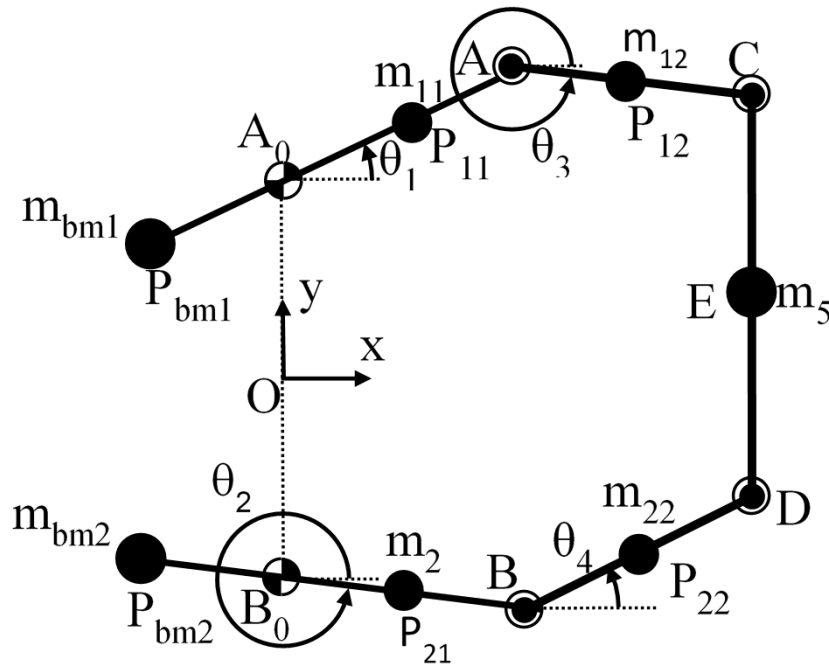
$$\begin{matrix} m_1 e_1 + m_2 (1 - \frac{e_2}{l_2}) l_1 = 0 & m_1 f_1 - m_2 \frac{f_2}{l_2} l_1 = 0 \\ m_3 (l_3 - e_3) + m_2 \frac{e_2}{l_2} l_3 = 0 & m_3 f_3 - m_2 \frac{f_2}{l_2} l_3 = 0 \end{matrix}$$

Paralelkenarlı 6-çubuk mekanizması



Paralel uzuvların momentum değişimleri kümülatif olacağından yan kollar (H_0H, HJ, K_0K, KL) iç kollara toplanmıştır. Ara kolların ise (AK ve BH) kütleleri yarım yarım olarak iç kollara toplanmıştır.

Paralelkenarlı 6-çubuk mekanizması



$$|A_0P_{bm1}| = |B_0P_{bm2}| = p_{bm}$$

$$|A_0B_0| = |CD| = a$$

$$|A_0P_{11}| = |B_0P_{21}| = p_1$$

$$|AP_{12}| = |BP_{22}| = p_2$$

$$m_{11} = m_{21} = m_1$$

$$m_{12} = m_{22} = m_2$$

$$m_{bm1} = m_{bm2} = m_{bm}$$

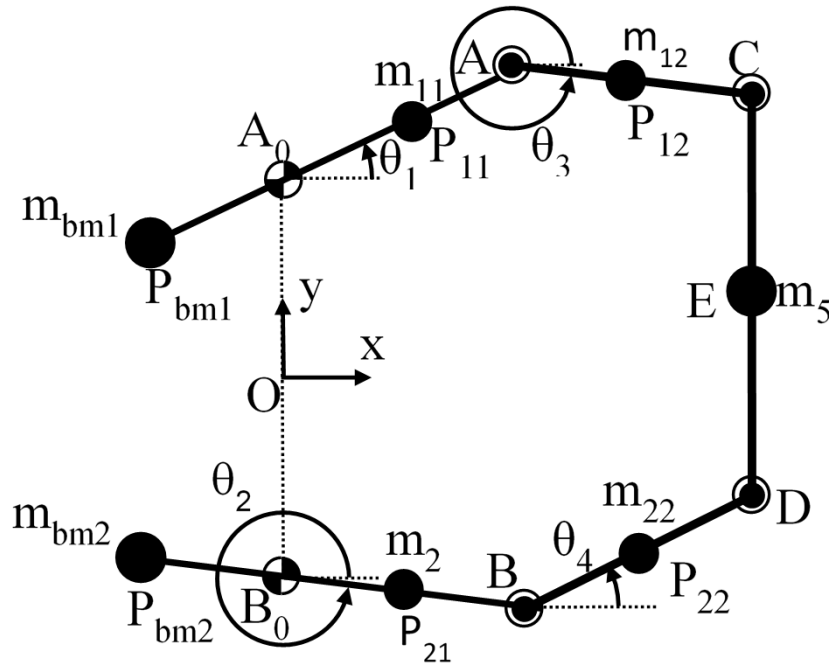
$$\theta_4 = \theta_1, \theta_3 = \theta_2$$

$$\bar{r}_{P_{11}} = p_1 e^{i\theta_1} = \begin{bmatrix} p_1 c\theta_1 \\ p_1 s\theta_1 \end{bmatrix} \Rightarrow \dot{\bar{r}}_{P_{11}} = \begin{bmatrix} -p_1 s\theta_1 \dot{\theta}_1 \\ p_1 c\theta_1 \dot{\theta}_1 \end{bmatrix}; \quad \bar{r}_{P_{12}} = re^{i\theta_1} + p_2 e^{i\theta_2} = \begin{bmatrix} rc\theta_1 + p_2 c\theta_2 \\ rs\theta_1 + p_2 s\theta_2 \end{bmatrix} \Rightarrow \dot{\bar{r}}_{P_{12}} = \begin{bmatrix} -rs\theta_1 \dot{\theta}_1 - p_2 s\theta_2 \dot{\theta}_2 \\ rc\theta_1 \dot{\theta}_1 + p_2 c\theta_2 \dot{\theta}_2 \end{bmatrix}$$

$$\bar{r}_{P_{21}} = p_1 e^{i\theta_2} = \begin{bmatrix} p_1 c\theta_2 \\ p_1 s\theta_2 \end{bmatrix} = \bar{r}_{P_{21}} = \begin{bmatrix} -p_1 s\theta_2 \dot{\theta}_2 \\ p_1 c\theta_2 \dot{\theta}_2 \end{bmatrix}; \quad \bar{r}_{P_{22}} = re^{i\theta_2} + p_2 e^{i\theta_1} = \begin{bmatrix} rc\theta_2 + p_2 c\theta_1 \\ rs\theta_2 + p_2 s\theta_1 \end{bmatrix} \Rightarrow \dot{\bar{r}}_{P_{22}} = \begin{bmatrix} -rs\theta_2 \dot{\theta}_2 - p_2 s\theta_1 \dot{\theta}_1 \\ rc\theta_2 \dot{\theta}_2 + p_2 c\theta_1 \dot{\theta}_1 \end{bmatrix}$$

$$\bar{r}_5 = re^{i\theta_1} + re^{i\theta_2} = \begin{bmatrix} rc\theta_1 + rc\theta_2 \\ rs\theta_1 + rs\theta_2 \end{bmatrix} \Rightarrow \dot{\bar{r}}_5 = \begin{bmatrix} -rs\theta_1 \dot{\theta}_1 - rs\theta_2 \dot{\theta}_2 \\ rc\theta_1 \dot{\theta}_1 + rc\theta_2 \dot{\theta}_2 \end{bmatrix}; \quad \bar{L} = m_1 \dot{\bar{r}}_{P_{11}} + m_2 \dot{\bar{r}}_{P_{12}} + m_5 \dot{\bar{r}}_5 + m_1 \dot{\bar{r}}_{P_{21}} + m_2 \dot{\bar{r}}_{P_{22}}$$

Paralelkenarlı 6-çubuk mekanizması



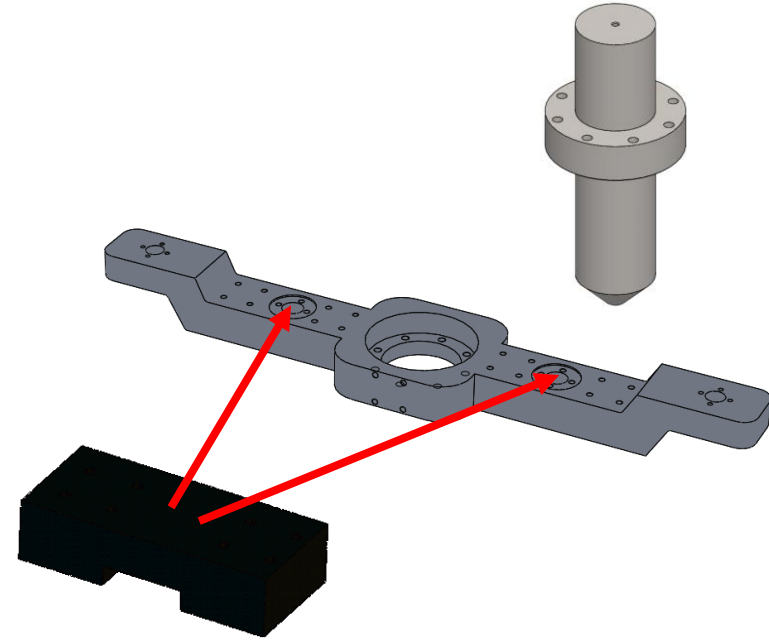
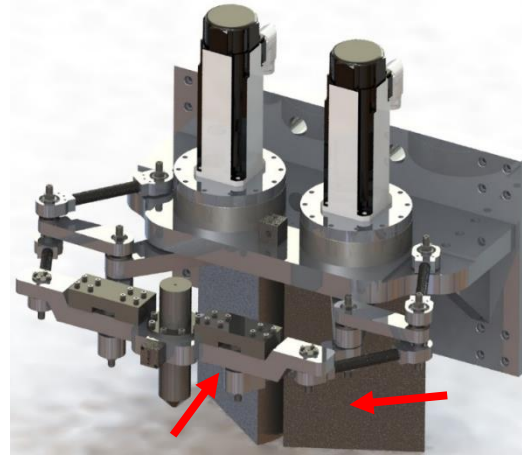
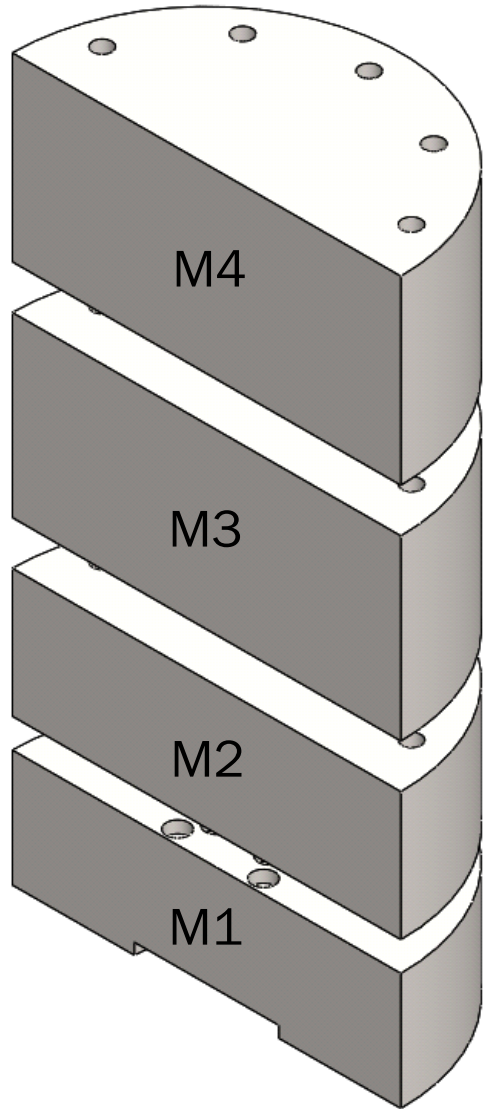
$$\begin{aligned}
 |A_0P_{bm1}| &= |B_0P_{bm2}| = p_{bm} \\
 |A_0B_0| &= |CD| = a \\
 |A_0P_{11}| &= |B_0P_{21}| = p_1 \\
 |AP_{12}| &= |BP_{22}| = p_2 \\
 m_{11} &= m_{21} = m_1 \\
 m_{12} &= m_{22} = m_2 \\
 m_{bm1} &= m_{bm2} = m_{bm}
 \end{aligned}$$

$$\bar{L} = m_1 \dot{r}_{P_{11}} + m_2 \dot{r}_{P_{12}} + m_5 \dot{r}_5 + m_1 \dot{r}_{P_{21}} + m_2 \dot{r}_{P_{22}}$$

$$= \begin{bmatrix} (-m_1 p_1 - (m_2 + m_5)r - m_2 p_2) \sin \theta_1 \\ (m_1 p_1 + (m_2 + m_5)r + m_2 p_2) \cos \theta_1 \end{bmatrix} \dot{\theta}_1 + \begin{bmatrix} (-m_2 p_2 - (m_5 + m_2)r - m_1 p_1) \sin \theta_2 \\ (m_2 p_2 + (m_5 + m_2)r + m_1 p_1) \cos \theta_2 \end{bmatrix} \dot{\theta}_2$$

$$\bar{L} = \sum_{i=1}^2 m_{bm} \dot{r}_{b_{mi}} = \begin{bmatrix} m_{bm} p_{bm} \sin \theta_1 \\ -m_{bm} p_{bm} \cos \theta_1 \end{bmatrix} \dot{\theta}_1 + \begin{bmatrix} m_{bm} p_{bm} \sin \theta_2 \\ -m_{bm} p_{bm} \cos \theta_2 \end{bmatrix} \dot{\theta}_2 \Rightarrow m_1 p_1 + (m_2 + m_5)r + m_2 p_2 = -m_{bm} p_{bm}$$

Dengeleme Kütelleri Tasarımı



M1 + M2: Sadece platform dengeleme

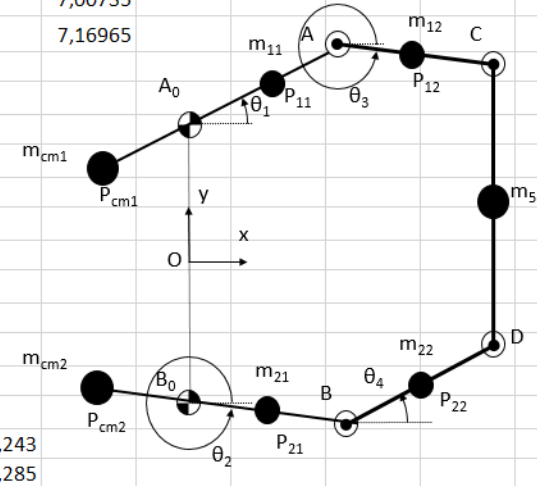
M1 + M2 + M3: platform + uç işlemci dengeleme

M1 + M2 + M3 + M4: 5 kg dengeleme

Yük	Dengeleme kütelleri
1.45 kg	$M_1 + M_2 = 10.1 \text{ kg}$
3.41 kg	$M_1 + M_2 + M_3 = 17.1 \text{ kg}$
5 kg	$M_1 + M_2 + M_3 + M_4 = 24.28 \text{ kg}$

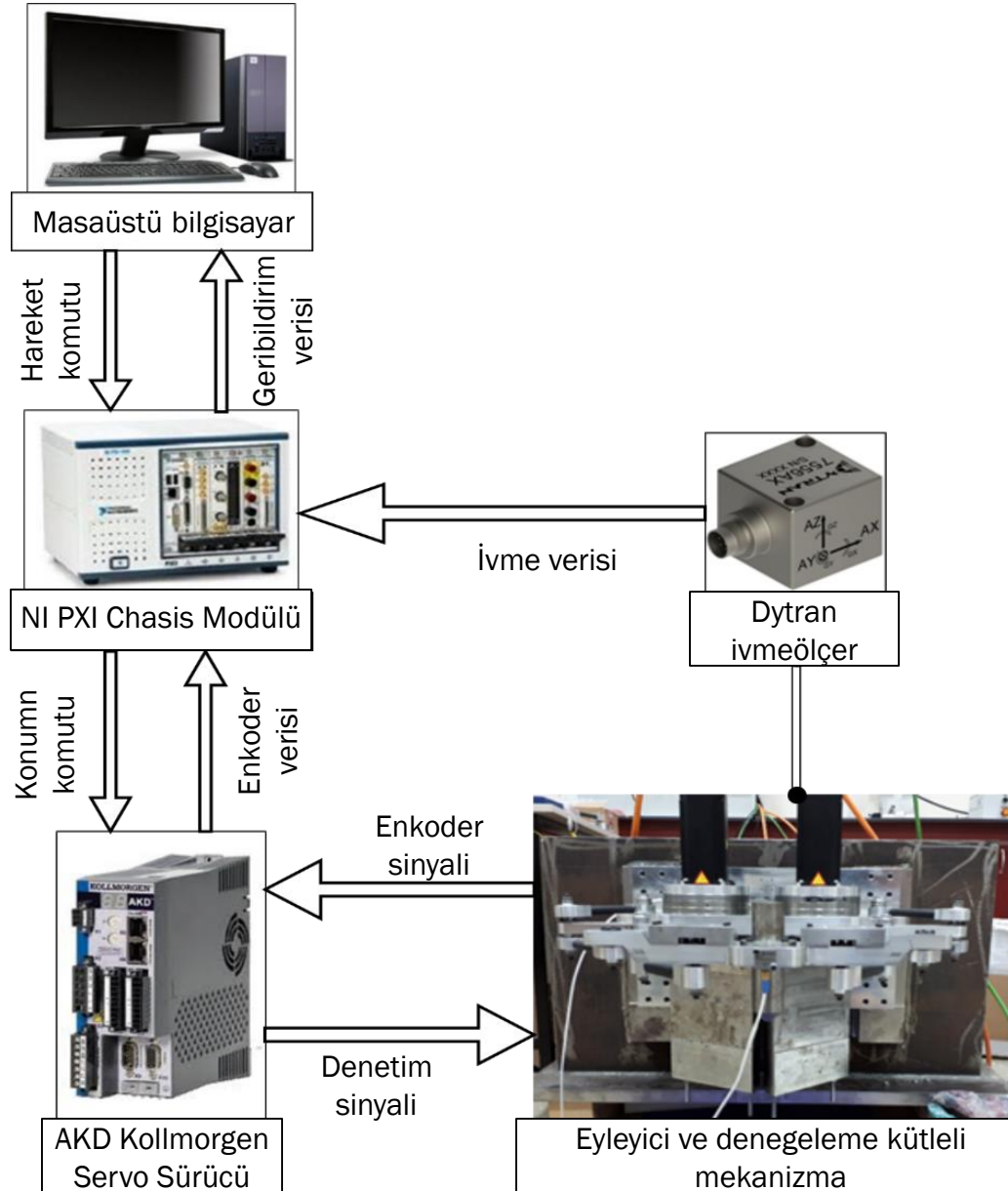
Dengeleme Hesabı

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
1	m11=m21	1,04642 kg			p11=p21	0,05943 m		r	0,15 m			m11	1,181		Slik	60,4 g	
2	m12=m22	0,58909 kg			p12=p22	0,0187 m						m22	0,34		saplama	462,65 g	
3	m3	5 kg															
4											DK						
5			m_{cm1}/m_{cm2}	p_{cm1}/p_{cm2}				miller+platform	1451 g		10,099 kg						
6	$m_{cm1} \cdot p_{cm1}$	-0,9116	24,2761	-0,03755				uç işlemci ile	3411,6 g		17,1064 kg		7,00735				
7	$m_{cm2} \cdot p_{cm2}$	-0,9116						5 kg	5000 g		24,276 kg		7,16965				
8																	
9	7075 Al Volume	13190 cm ³															
10	7075Al mass	37 g															
11	7075Al density	0,00281 g/cm ³															
12																	
13	Steel Volume	238692 cm ³			mass1	mass2	mass3	mass4	Toplam								
14	Steel Mass	1870 g			5027,46	5064,21	7018,82	7152,084471	24262,567	0,0135504							
15	Steel Density	0,00783 g/cm ³															
16					1	5027,46											
17	5000Al Volume	2147116 cm ³			2	5064,21											
18	5000Al Mass	5684 g			3	10091,7											
19	5000Al Density	2,64727 kg/m ³			4	7018,82											
20						17110,5											
21						7152,08											
22	Uzuvlar	Uzunluk (mm)				24262,6											
23	$IA_0A_1=IB_0B_1$	$l_1=l_2=150$															
24	$IAE_1=IBE_1$	$l_3=l_4=150$															
25	$IA_0P_{11}=IB_0P_{21}$	$r_1=r_2=33.6$															
26	$IAP_{12}=IBP_{22}$	$r_3=r_4=75$															
27	$IA_0P_{cm1}=IB_0P_{cm2}$	$r_{c1}=r_{c2}=79.7$															



	Kütle (kg)	Atalet (kg.mm ²)	
m11=m21	1,168	18485,246	0,01849
m12=m22	0,267	3340,247	0,00334
m5	5		0
mcm1=mcm2	10,658	83028,667	0,08303

Dengeleme Testleri (İvme-ölçer ile)

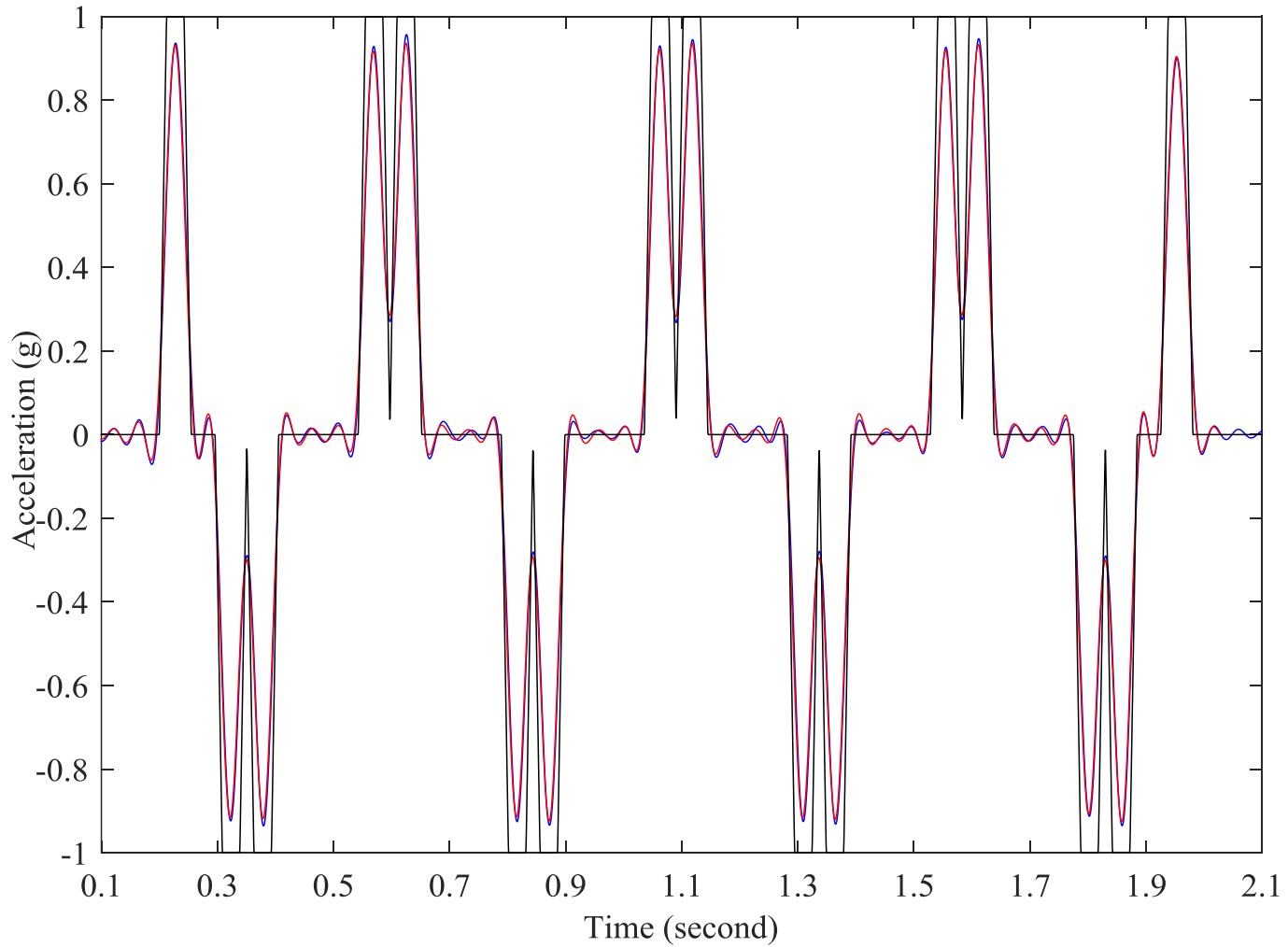


Dengeleme Testleri (İvme-ölçer ile)

Yük	Dengeleme Kütlesi	İvme (g: 9.81 m/s ²)
Sadece platform (1.45 kg)	10.1 kg	1g, 2g, 3g, 4g
platform + uç işlemci (3.41 kg)	17.1 kg	0.5g, 1g, 2g, 3g, 3.5g
platform + uç işlemci + ekstra kütleler (5 kg)	24.28 kg	0.5g, 1g, 2g, 3g, 3.5g

Platform hareketi: önce ± 40 mm dikey hareket, sonra ± 40 mm yatay hareket

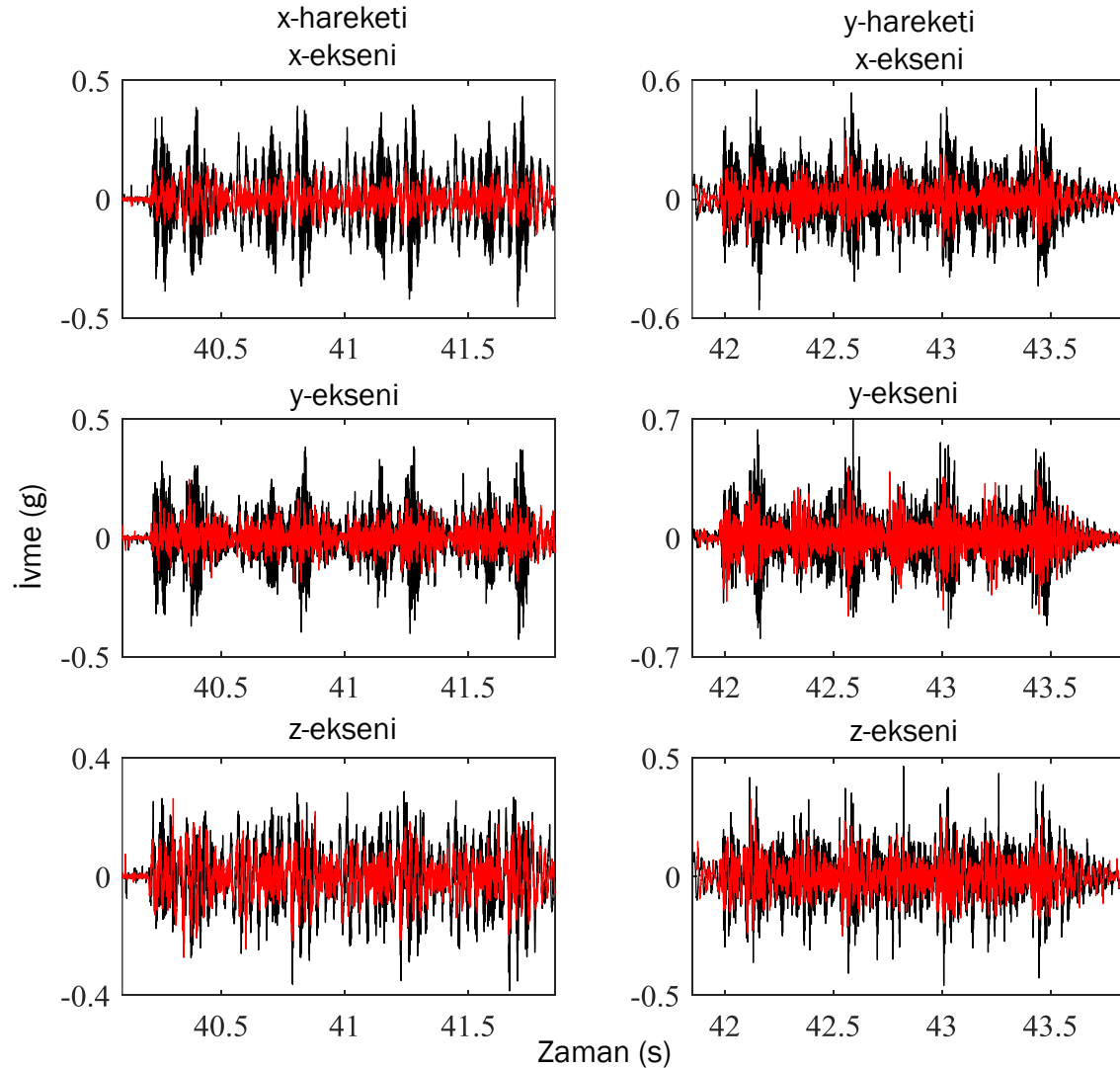
Dengeleme Testleri (İvme-ölçer ile)



İvmeölçer verisi Enkoder verisinden hesaplanan Hedef veri

İvme komutu başarımı - Azami 1g ivme ile platform hareketi

Dengeleme Testleri (İvme-ölçer ile)



Dengelemeli-dengelemesiz karşılaştırma / 5 kg platform / Azami 3g ivme

Dengeleme Testleri (İvme-ölçer ile)

	İvme	x-ekseni	y-ekseni	z-ekseni
x-hareketi	1 g	52.31 %	43.77 %	35.57 %
	2 g	44.45 %	39 %	33.61 %
	3 g	40.77 %	34.37 %	37.57 %
	4 g	50.94 %	34.66 %	29.40 %
y-hareketi	1 g	49.85 %	54.58 %	46.1 %
	2 g	44.32 %	54.41 %	42.52 %
	3 g	43.07 %	52.45 %	41.15 %
	4 g	41.59 %	29.02 %	34.99 %

Dengeleme sonrası ivme genliklerindeki düşüşler – Sadece platform ile

Dengeleme Testleri (İvme-ölçer ile)

	İvme	x-ekseni	y-ekseni	z-ekseni
x-hareketi	0.5 g	73.06 %	58.54 %	37.42 %
	1 g	70.93 %	51.83 %	43.2 %
	2 g	70.48 %	53.29 %	41.29 %
	3 g	72.37 %	49.14 %	45.06 %
	3.5 g	68.72 %	40.22 %	28.61 %
y-hareketi	0.5 g	62.70 %	50.73 %	47.72 %
	1 g	71.4 %	54.71 %	51.87 %
	2 g	70.65 %	57.95 %	52.22 %
	3 g	66.56 %	50.97 %	44.92 %
	3.5 g	55.04 %	35.16 %	33.29 %

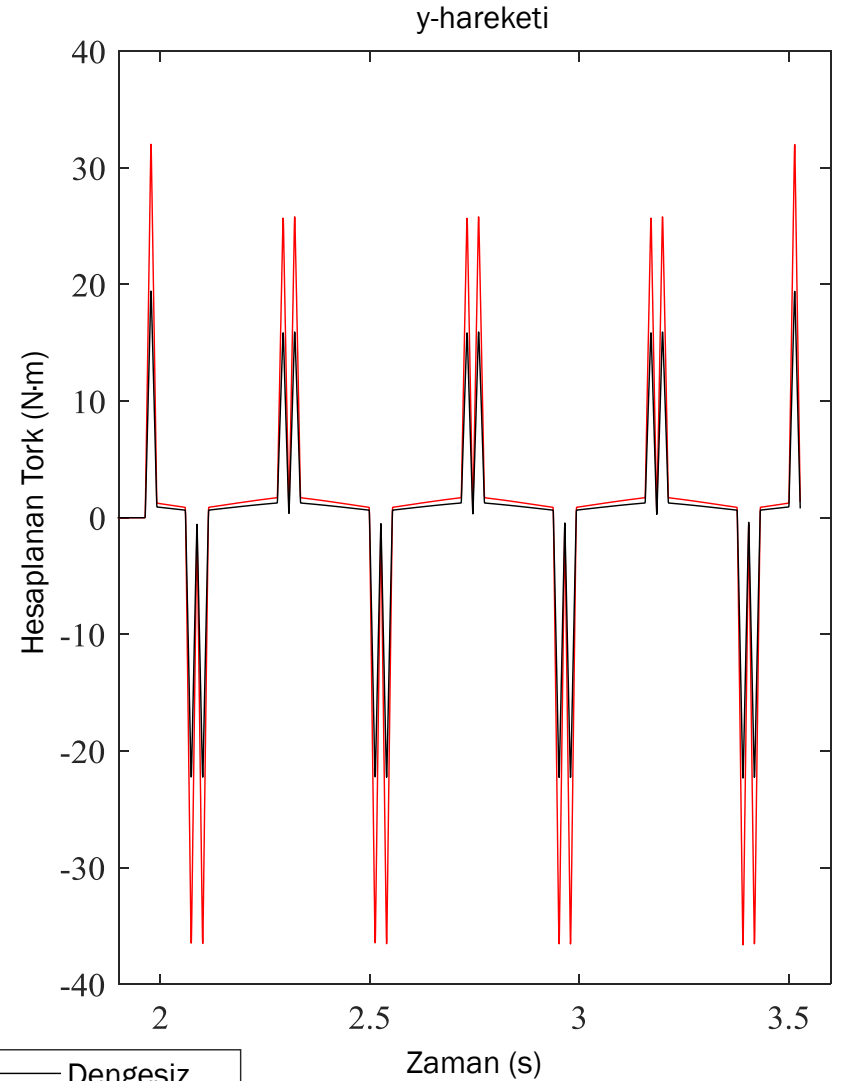
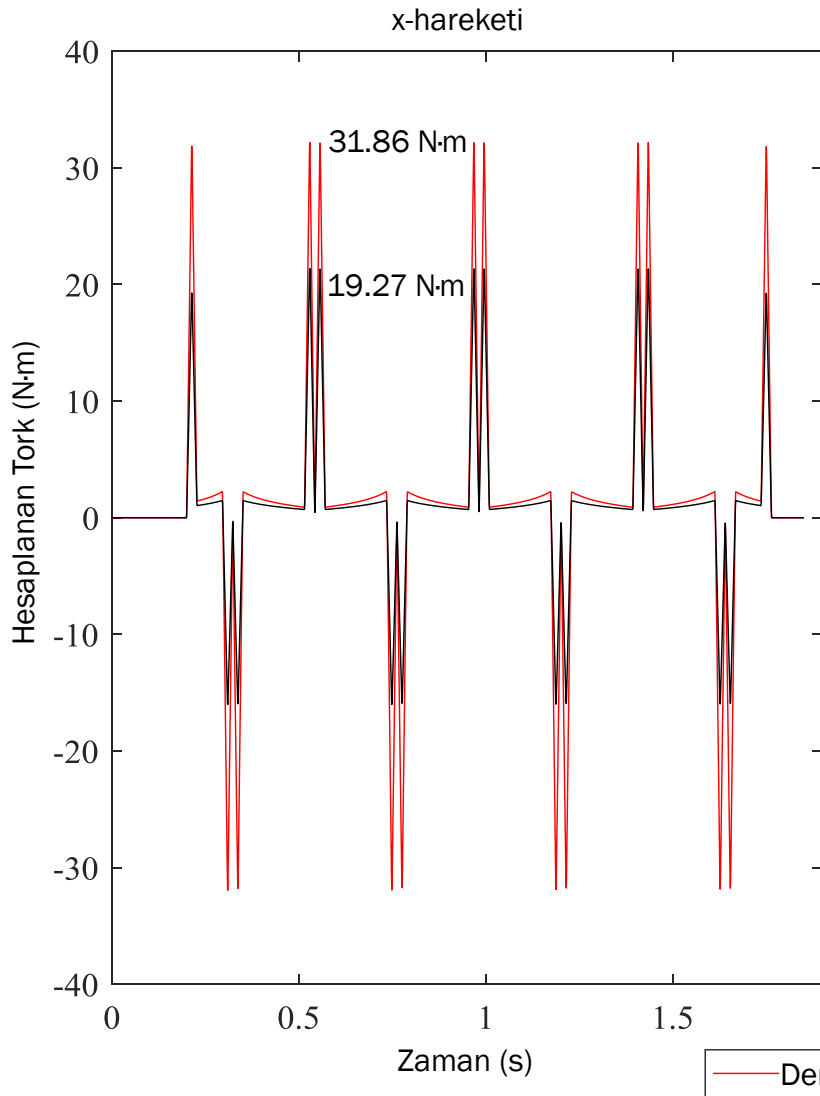
Dengeleme sonrası ivme genliklerindeki düşüşler – Platform + uç işlemci ile

Dengeleme Testleri (İvme-ölçer ile)

	İvme	x-ekseni	y-ekseni	z-ekseni
x-hareketi	0.5 g	66.38 %	59.2 %	40.24 %
	1 g	64.73 %	56.33 %	28.01 %
	2 g	53.11 %	54.95 %	30.19 %
	3 g	62.76 %	51.42 %	35.24 %
y-hareketi	0.5 g	60.84 %	51.64 %	37.16 %
	1 g	69.35 %	56.39 %	36.27 %
	2 g	68.31 %	65.90 %	42.78 %
	3 g	53.19 %	35.72 %	34.04 %

Dengeleme sonrası ivme genliklerindeki düşüşler - 5 kg ile

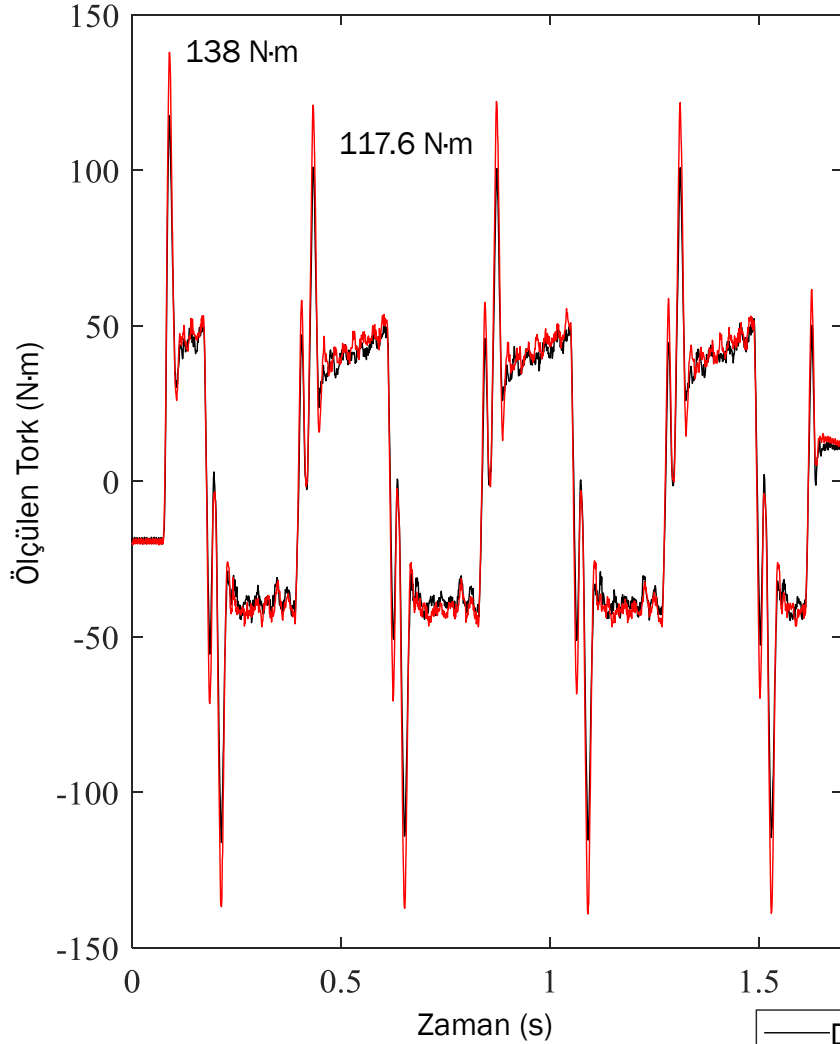
Dengeleme Testleri – Tork Değerleri



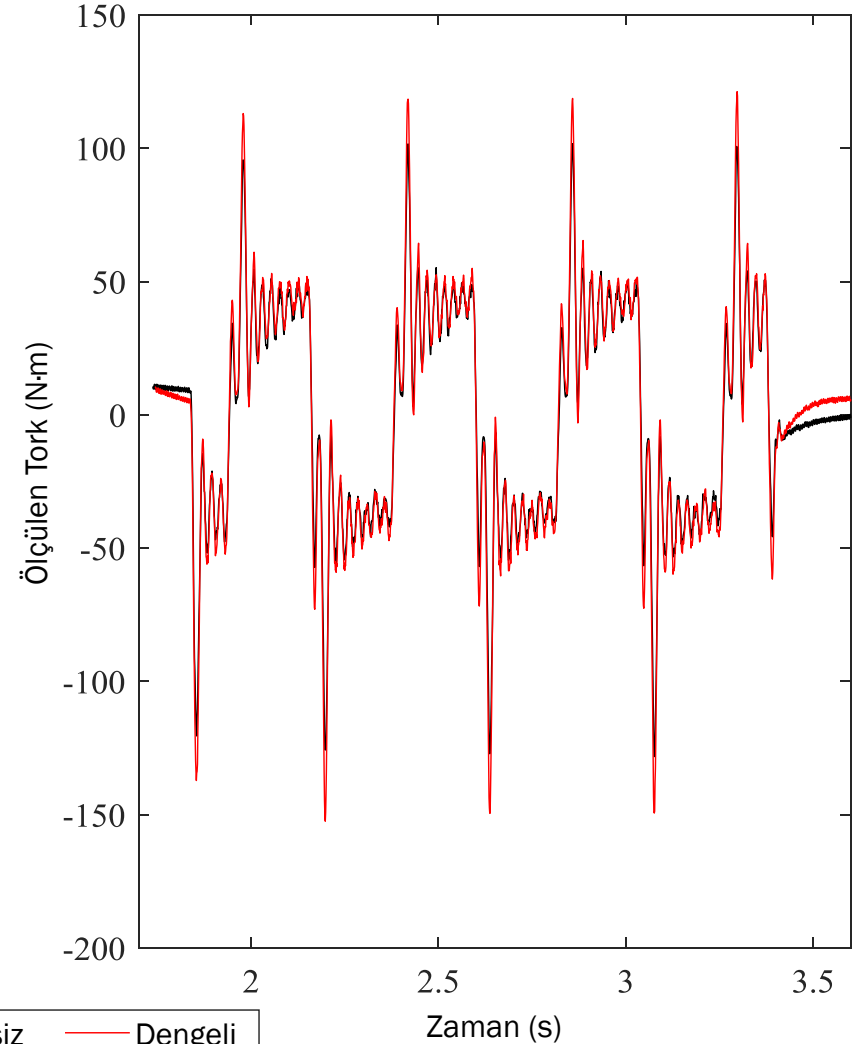
Dengelemeli-dengelemesiz karşılaştırma / 5 kg platform / Azami 3g ivme

Dengeleme Testleri – Tork Değerleri

x-hareketi

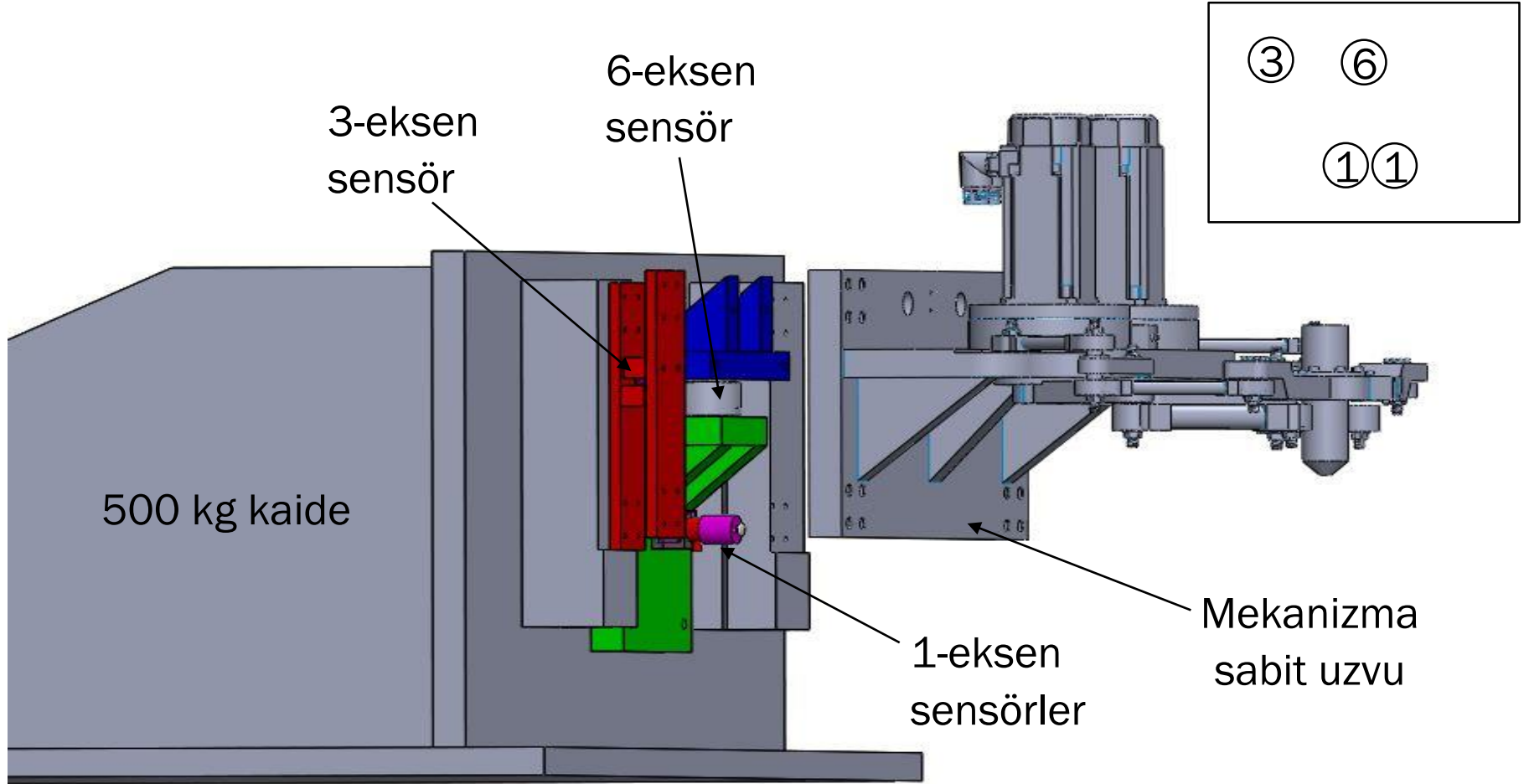


y-hareketi



Dengelemeli-dengelemesiz karşılaştırma / 5 kg platform / Azami 3g ivme

Dengeleme Testleri (Kuvvet-ölçer ile)



Mekanizma grubu ile kaide arasında 4 kuvvet-ölçer var

Dengeleme Testleri (Kuvvet-ölçer ile)

Kuvvet-ölçerler:

6-eksen kuvvet-ölçer: ME-K6D40; kapasite:

x- ve y- ekseninde ± 500 N, z-ekseninde ± 2000 N

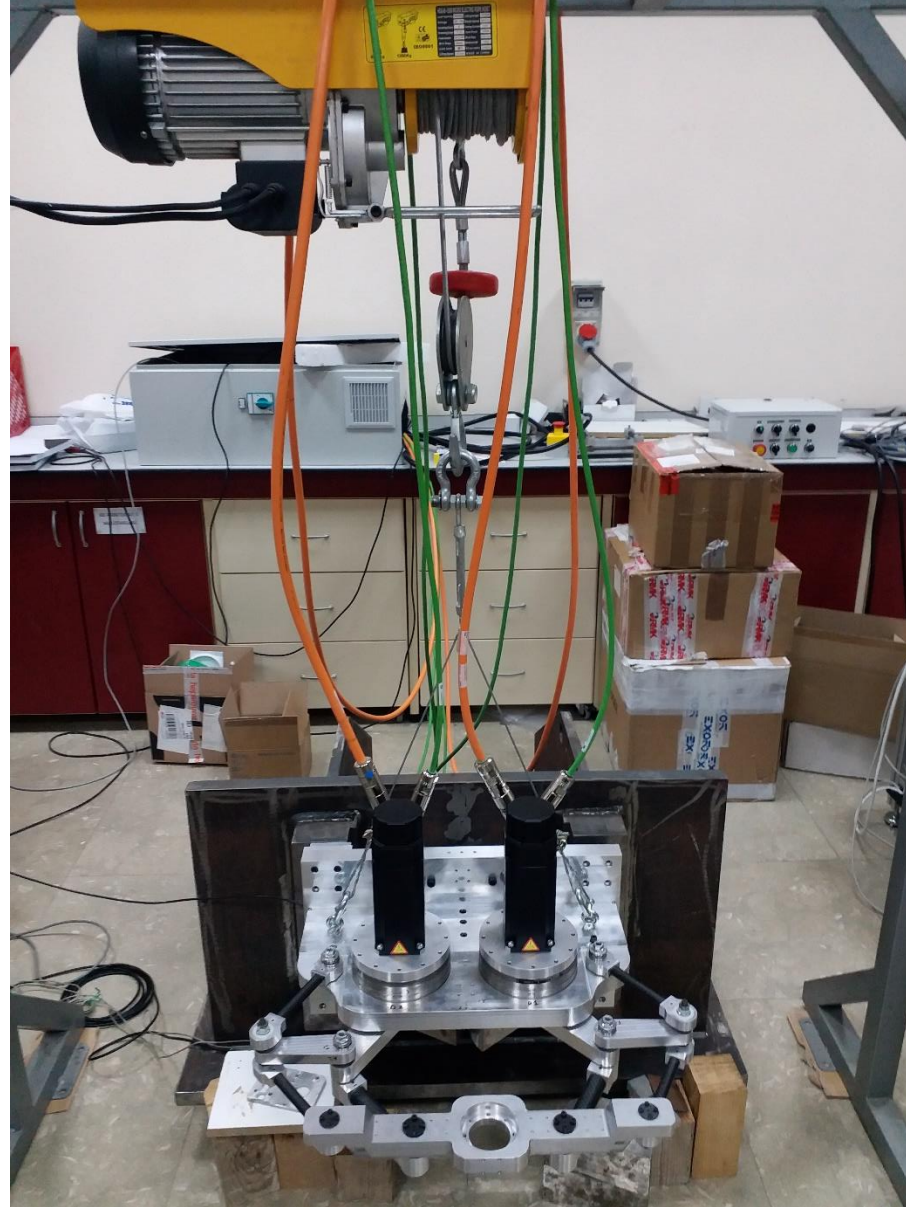
3 eksende 20 N·m moment

3-eksen kuvvet-ölçer: Kistler 9016-b; kapasite: 3 ekseninde ± 2000 N

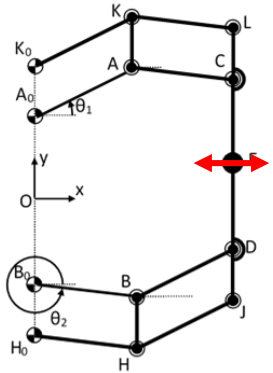
1-eksen kuvvet-ölçerler: Futek FSH03886; kapasite: ± 1112 N

Platform hareketi: 1) ± 40 mm dikey hareket,
2) ± 40 mm yatay hareket, 3) boyu 40 mm, eni 50 mm olan üçgen

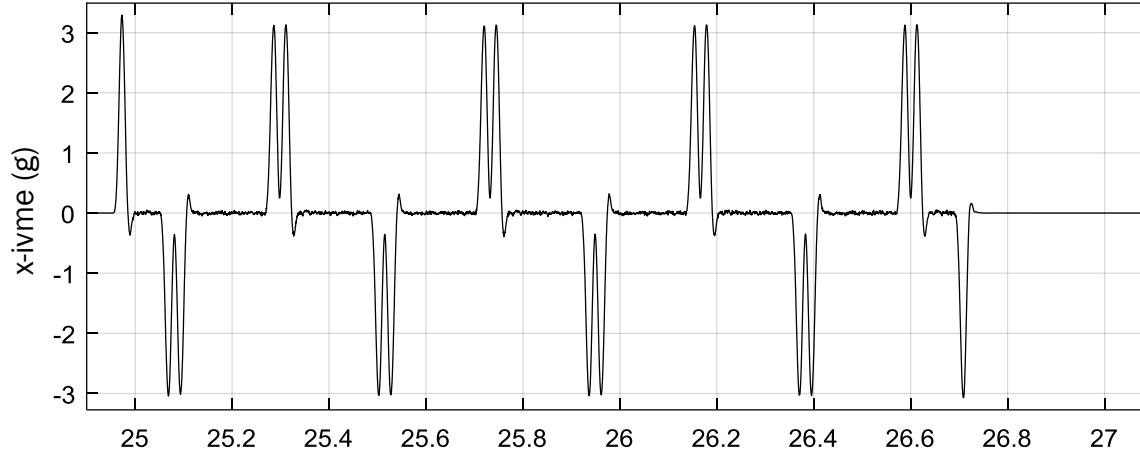
Dengeleme Testleri (Kuvvet-ölçer ile)



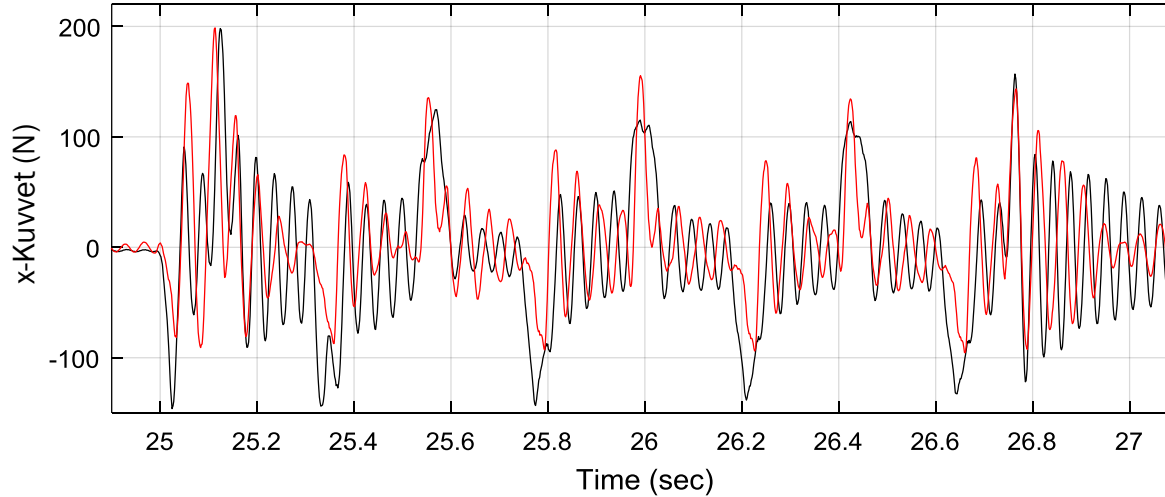
Dengeleme Testleri (Kuvvet-ölçer ile)



İvme min/max: [-3.07, 3.29]



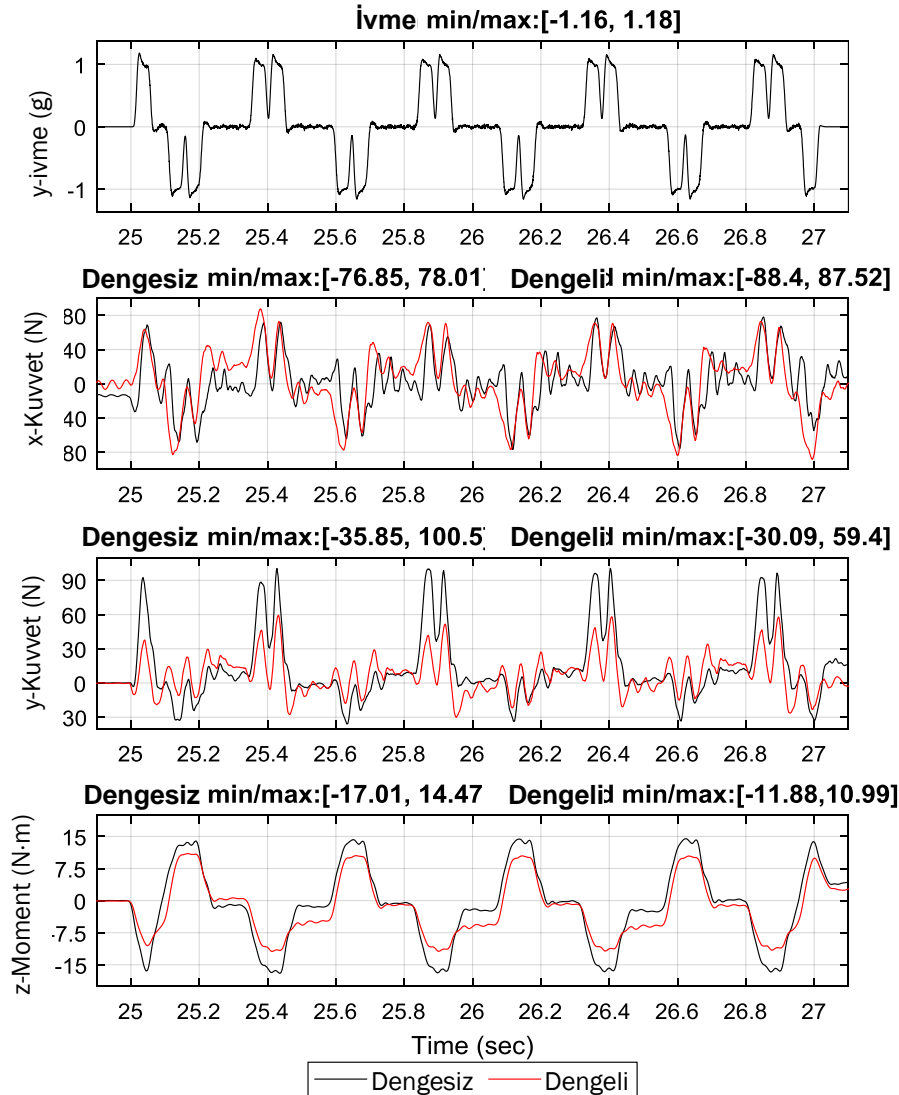
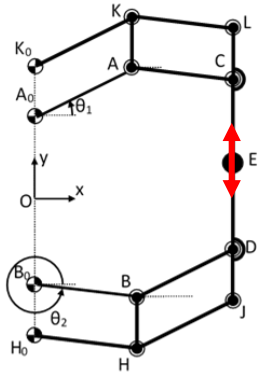
Dengesiz min/max: [-146.1, 198.1] Dengelil min/max: [-95.45, 198.6]



— Dengesiz — Dengeli

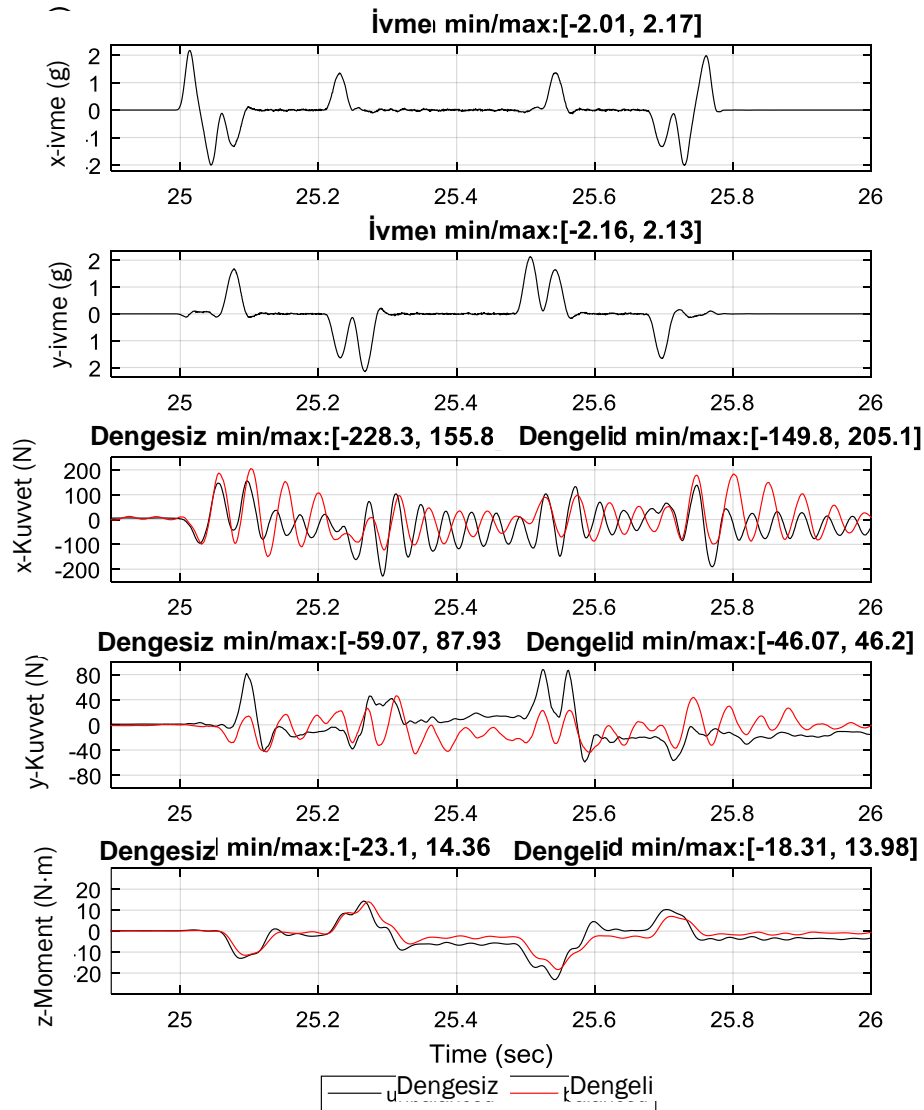
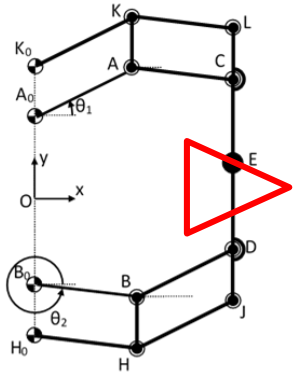
x-ekseni hareketi / 5 kg platform / Azami 3g ivme

Dengeleme Testleri (Kuvvet-ölçer ile)



y-ekseni hareketi / 5 kg platform / Azami 1g ivme

Dengeleme Testleri (Kuvvet-ölçer ile)



Üçgen hareketi / 5 kg platform / Azami 1g ivme